

Course Code: EC409

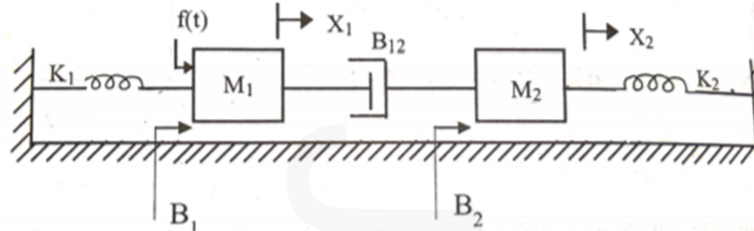
Course Name: CONTROL SYSTEMS

Max. Marks: 100

Duration: 3 Hours

*(Graph sheet and semi- log sheets will be provided)***PART A***Answer any two full questions, each carries 15 marks*

1. a) Determine the transfer function of the system $X_2(s)/F(s)$ (6)



- b) Draw the signal flow graph for the following set of algebraic equations (9)

$x_2 = x_1 + ax_5$, $x_3 = bx_2 + cx_4$, $x_4 = dx_2 + ex_3$, $x_5 = fx_4 + gx_3$, $x_6 = x_5$. Hence find the overall transfer function using Mason's gain formula

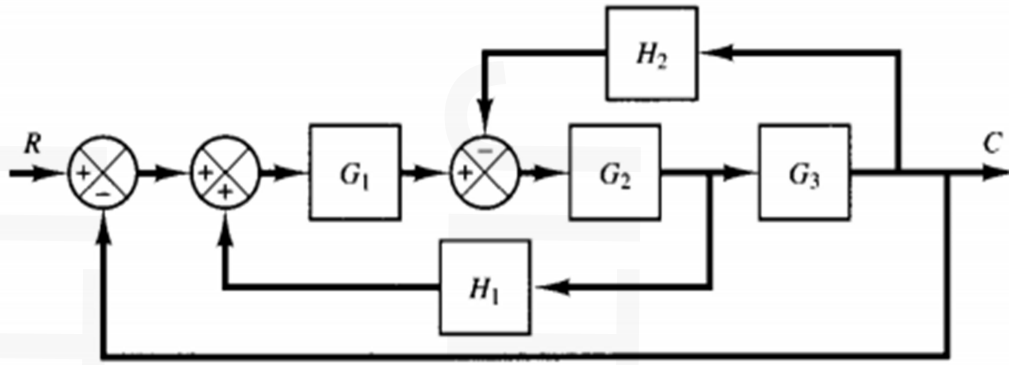
2. a) Open loop transfer function of a unity feedback system is

$$G(s) = \frac{10}{s(s+5)(s+10)}$$

the input $r(t) = 5 + 10t + 6t^2$ (8)

- b) Derive an expression for time response of a critically damped second order system to impulse input (7)

3. a) Reduce the block diagram using block reduction technique and find $C(s)/R(s)$ (8)



- b) Explain various time domain specifications with neat sketch and mention the corresponding equations also. (7)

PART B

Answer any two full questions, each carries 15 marks.

4. a) Draw the bode plot for $G(s)H(s) = \frac{10(s+100)}{s(s+5)(s+2)}$ Find gain margin and phase margin and hence comment on the stability of the system. (12)
- b) Find damping ratio and natural frequency of oscillation of a second order system whose closed loop transfer function is given by $\frac{C(s)}{R(s)} = \frac{9}{s^2 + 6s + 9}$. (3)
5. a) Construct Routh array and determine the stability of the system represented by the characteristic equation $S^6 + 2S^5 + S^4 + 2S^3 + S^2 + 2s + 1 = 0$. Comment on the location of roots in s plane (8)
- b) Describe the design procedure of lead compensator (7)
6. a) Sketch the root locus whose open loop transfer function is (12)

$$G(s) = \frac{K}{s(s+1.5)(s+4)}$$

and comment on the stability of the system.

- b) Explain frequency domain specification with the help of bode plot and state the condition for stability. (3)

PART C

Answer any two full questions, each carries 20 marks

7. a) Consider the system with state equation

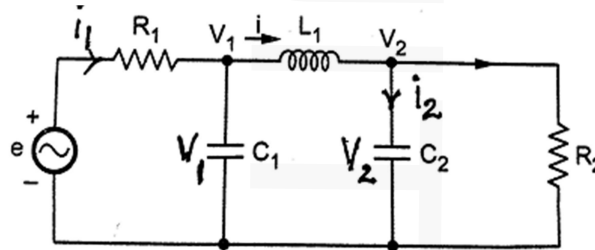
$$\begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \\ \dot{X}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ X_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} U .$$

- Estimate state controllability by Gilbert Test (8)

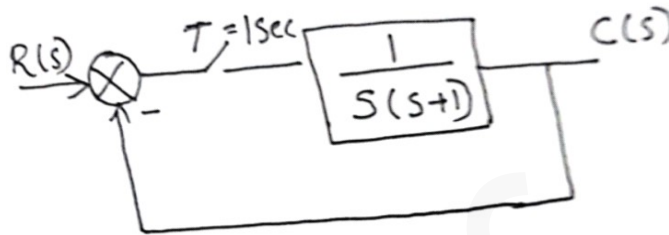
b) What are the properties of state transition matrix . Find the time response of a

system whose $A = \begin{bmatrix} 1 & -1 \\ 0 & -2 \end{bmatrix}$ and $X(0) = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$ (7)

c) Obtain the state model of given electrical system (5)



8. a) Find the pulse transfer function for the error sampled system shown in figure.



(10)

b) Solve the difference equation $c(k+2)+3c(k+1)+2c(k)=u(k)$, where $c(0)=1$; $c(1)=-3$; $c(k)=0$ for $k < 0$. Determine Z transform (10)

9. a) Obtain the state equation and output equation in phase variable form

$$\frac{Y(s)}{U(s)} = \frac{6s^2 + 12s + 6}{s^3 + 6s^2 + 10s + 4} \quad (10)$$

b) Check for stability of sampled data control system represented by

$$F(z) = z^4 - 1.8z^3 + 1.09z^2 - 0.26z + 0.025 = 0. \text{ Use Jury's test}$$

(10)
